

The following Listing of Claims will replace all prior versions, and listings, of claims in the application.

**LISTING OF CLAIMS:**

1. (Currently Amended) A method of modeling flame propagation comprising:  
defining a flame surface area density of a flame as a flame surface area per unit  
volume of the flame;

expressing flame progress as generation of the flame surface area density in terms of  
at least one of a turbulent combustion and a laminar combustion;

determining flame growth resulting from turbulent combustion ~~as being inversely  
proportional to a chemical reaction characteristic time and~~ as a function of a turbulent  
Reynolds number; and

modeling the flame propagation based on the flame growth; and  
optimizing combustion within a combustion chamber using the flame propagation.

2. (Original) The flame propagation modeling method as recited in claim 1,  
further comprising

determining the flame growth resulting from laminar combustion as being  
proportional to both a laminar flame speed and to a ratio of a temperature of a burned portion  
to a temperature of an unburned portion and as a function of the Karlowitz number.

3. (Original) The flame propagation modeling method as recited in claim 1,  
wherein

the generation of the flame surface area density is expressed as a combination of the  
turbulent combustion and the laminar combustion.

4. (Currently Amended) The flame propagation modeling method as recited in  
claim 1, wherein

the flame growth resulting from the turbulent combustion is calculated based on the  
flame growth being ~~inversely proportional to the chemical reaction characteristic time and~~

proportional to both the turbulent Reynolds number raised to an exponential power and a stretch rate of the flame.

5. (Original) The flame propagation modeling method as recited in claim 2, wherein

the flame generation is further expressed as transport of the flame surface area density, which is expressed in terms of flame growth resulting from turbulent combustion and flame growth resulting from laminar combustion; and

the flame growth resulting from laminar combustion being expressed as proportional to the laminar flame speed, to the ratio of the temperature of a burned portion to the temperature of an unburned portion, and to an exponential function of the Karlowitz number.

6. (Original) The flame propagation modeling method as recited in claim 5, wherein

the exponential function of the Karlowitz number is the base of the natural logarithm raised to the power of the Karlowitz number.

7. (Original) The flame propagation modeling method as recited in claim 1, wherein

the flame growth resulting from the turbulent combustion is expressed as follows:

$$S_T = \alpha_1 (Re_t)^{\alpha_2} \Gamma \frac{\varepsilon}{\kappa} \Sigma,$$

where  $S_T$  represents flame growth resulting from turbulent combustion,  $\Sigma$  represents flame surface area density,  $k$  represents turbulence strength,  $\varepsilon$  represents turbulence dissipation rate,  $Re_t$  represents turbulent Reynolds number,  $\Gamma$  represents flame stretch rate, and  $\alpha_1$  and  $\alpha_2$  are model constants.

8. (Original) The flame propagation modeling method as recited in claim 2, wherein

the flame growth resulting from the laminar combustion is expressed as follows:

$$S_L = \beta_1 \exp(-\beta_2 Ka) \frac{T_b}{T_u} U_L \Sigma^2,$$

where  $S_L$  flame growth resulting from laminar combustion,  
 $\Sigma$  represents flame surface area density,  $U_L$  represents laminar flame speed,  
 $T_b$  represents burned gas temperature,  $T_u$  represents unburned gas temperature,  $Ka$  represents  
Karlowitz number, and  $\beta_1$  and  $\beta_2$  are model constants.

9. (Original) The flame propagation modeling method as recited in claim 1,  
wherein

the flame generation is further expressed as transport of the flame surface area density,  
which is expressed in terms of flame growth resulting from turbulent combustion and flame  
growth resulting from laminar combustion; and

the flame generation is suppressed by a resistance force imposed by air.

10. (Original) The flame propagation modeling method as recited in claim 1,  
wherein

transport, generation, and diffusion of the flame surface area density are expressed as  
follows:

$$\frac{\partial \Sigma}{\partial t} + \frac{\partial u_i \Sigma}{\partial x_i} = \frac{\partial}{\partial x_i} \left( \frac{\nu_t}{\sigma_c} \frac{\partial \Sigma}{\partial x_i} \right) + \alpha_1 (Re_t)^{\alpha_2} \Gamma \frac{\varepsilon}{\kappa} \Sigma + \beta_1 \exp(-\beta_2 Ka) \frac{T_b}{T_u} U_L \Sigma^2 - D,$$

where  $\Sigma$  represents flame surface area density,  $k$  represents turbulence strength,  $\varepsilon$   
represents turbulence dissipation rate,  $Re_t$  represents turbulent Reynolds number,  $\Gamma$  represents  
flame stretch rate,  $U_L$  represents laminar flame speed,  $T_b$  represents burned gas temperature,  
 $T_u$  represents unburned gas temperature,  $Ka$  represents Karlowitz number,  $\nu_t$  represents  
turbulent kinematic viscosity,  $\sigma_c$  represents turbulent Schmidt number,  
 $D$  represents air resistance force, and  $\alpha_1$ ,  $\alpha_2$ ,  $\beta_1$  and  $\beta_2$  are model constants.

11. (Currently Amended) A method of modeling flame propagation comprising:  
defining a flame surface area density of a flame as a flame surface area per unit  
volume of the flame;

expressing flame progress as generation of the flame surface area density in terms of at least one of a turbulent combustion and a laminar combustion;

determining flame growth resulting from laminar combustion as being proportional to both a laminar flame speed and to a ratio of a temperature of a burned portion to a temperature of an unburned portion and as a function of the Karlowitz number; ~~and~~

modeling the flame propagation based on the flame growth; and

optimizing combustion within a combustion chamber using the flame propagation.

12. (Original) The flame propagation modeling method as recited in claim 11, wherein

the generation of the flame surface area density is expressed as a combination of the turbulent combustion and the laminar combustion.

13. (Currently Amended) The flame propagation modeling method as recited in claim 12, further comprising

determining flame growth resulting from the turbulent combustion is calculated based on a flame growth being ~~inversely proportional to a chemical reaction characteristic time~~ and proportional to both a turbulent Reynolds number raised to an exponential power and a stretch rate of the flame.

14. (Original) The flame propagation modeling method as recited in claim 11, wherein

the flame generation is further expressed as transport of the flame surface area density, which is expressed in terms of flame growth resulting from turbulent combustion and flame growth resulting from laminar combustion; and

the flame growth resulting from laminar combustion being expressed as proportional to the laminar flame speed, to the ratio of the temperature of a burned portion to the temperature of an unburned portion, and to an exponential function of the Karlowitz number.

15. (Original) The flame propagation modeling method as recited in claim 14, wherein

the exponential function of the Karlowitz number is the base of the natural logarithm raised to the power of the Karlowitz number.

16. (Original) The flame propagation modeling method as recited in claim 13, wherein

the flame growth resulting from the turbulent combustion is expressed as follows:

$$S_T = \alpha_1 (Re_t)^{\alpha_2} \Gamma \frac{\varepsilon}{\kappa} \Sigma,$$

where  $S_T$  represents flame growth resulting from turbulent combustion,  $\Sigma$  represents flame surface area density,  $k$  represents turbulence strength,  $\varepsilon$  represents turbulence dissipation rate,  $Re_t$  represents turbulent Reynolds number,  $\Gamma$  represents flame stretch rate, and  $\alpha_1$  and  $\alpha_2$  are model constants.

17. (Original) The flame propagation modeling method as recited in claim 16, wherein

the flame growth resulting from the laminar combustion is expressed as follows:

$$S_L = \beta_1 \exp(-\beta_2 Ka) \frac{T_b}{T_u} U_L \Sigma^2,$$

where  $S_L$  flame growth resulting from laminar combustion,  $\Sigma$  represents flame surface area density,  $U_L$  represents laminar flame speed,  $T_b$  represents burned gas temperature,  $T_u$  represents unburned gas temperature,  $Ka$  represents Karlowitz number, and  $\beta_1$  and  $\beta_2$  are model constants.

18. (Original) The flame propagation modeling method as recited in claim 11, wherein

the flame growth resulting from the laminar combustion is expressed as follows:

$$S_L = \beta_1 \exp(-\beta_2 Ka) \frac{T_b}{T_u} U_L \Sigma^2,$$

where  $S_L$  flame growth resulting from laminar combustion,  $\Sigma$  represents flame surface area density,  $U_L$  represents laminar flame speed,

$T_b$  represents burned gas temperature,  $T_u$  represents unburned gas temperature,  $Ka$  represents Karlowitz number, and  $\beta_1$  and  $\beta_2$  are model constants.

19. (Original) The flame propagation modeling method as recited in claim 11, wherein

the flame generation is further expressed as transport of the flame surface area density, which is expressed in terms of flame growth resulting from turbulent combustion and flame growth resulting from laminar combustion; and

the flame generation is suppressed by a resistance force imposed by air.

20. (Original) The flame propagation modeling method as recited in claim 11, wherein

transport, generation, and diffusion of the flame surface area density are expressed as follows:

$$\frac{\partial \Sigma}{\partial t} + \frac{\partial u_i \Sigma}{\partial x_i} = \frac{\partial}{\partial x_i} \left( \frac{\nu_i}{\sigma_c} \frac{\partial \Sigma}{\partial x_i} \right) + \alpha_1 (Re_t)^{\alpha_2} \Gamma \frac{\varepsilon}{\kappa} \Sigma + \beta_1 \exp(-\beta_2 Ka) \frac{T_b}{T_u} U_L \Sigma^2 - D,$$

where  $\Sigma$  represents flame surface area density,  $k$  represents turbulence strength,  $\varepsilon$  represents turbulence dissipation rate,  $Re_t$  represents turbulent Reynolds number,  $\Gamma$  represents flame stretch rate,  $U_L$  represents laminar flame speed,  $T_b$  represents burned gas temperature,  $T_u$  represents unburned gas temperature,  $Ka$  represents Karlowitz number,  $\nu_i$  represents turbulent kinematic viscosity,  $\sigma_c$  represents turbulent Schmidt number,  $D$  represents air resistance force, and  $\alpha_1$ ,  $\alpha_2$ ,  $\beta_1$  and  $\beta_2$  are model constants.